basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

DEPARTMENT OF BASIC EDUCATION
PRIVATE BAG X895, PRETORIA 0001
17 -11- 2024
APPROVED MARKING GUIDELINE
PUBLIC EXAMINATION

NATIONAL SENIOR CERTIFICATE/ *NASIONALE SENIOR SERTIFIKAAT*

GRADE 12/*GRAAD 12*

MATHEMATICS P2/*WISKUNDE V2*

NOVEMBER 2024

MARKING GUIDELINES/*NASIENRIGLYNE*

MARKS/*PUNTE*: 150

Approved
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Umalusi Moderator
14/11/2024

These marking guidelines consist of 25 pages./
Hierdie nasienriglyne bestaan uit 25 bladsye.

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Approved
2024-11-14

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed-out version.
- Consistent accuracy applies in ALL aspects of the Marking Guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

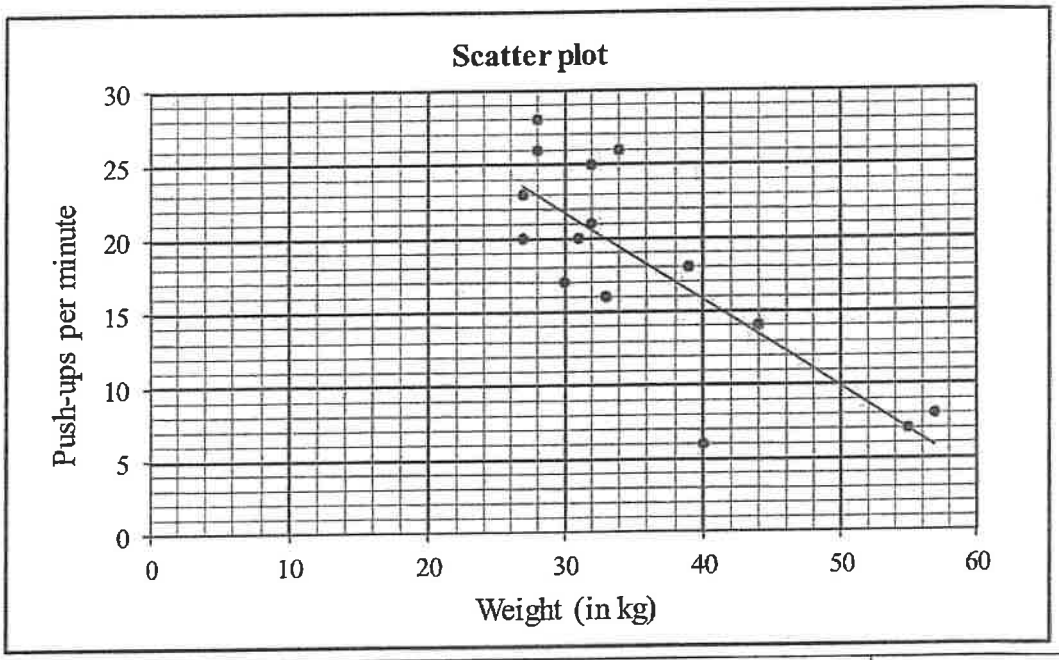
LET WEL:

- *As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.*
- *As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.*
- *Volgehoue akkuraatheid word in ALLE aspekte van die Nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.*
- *Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.*

GEOMETRY • MEETKUNDE	
S	**A mark for a correct statement** **(A statement mark is independent of a reason)**
	'n Punt vir 'n korrekte bewering **('n Punt vir 'n bewering is onafhanklik van die rede)**
R	**A mark for the correct reason** **(A reason mark may only be awarded if the statement is correct)**
	'n Punt vir 'n korrekte rede **('n Punt word slegs vir die rede toegeken as die bewering korrek is)**
S/R	**Award a mark if statement AND reason are both correct**
	Ken 'n punt toe as die bewering EN rede beide korrek is

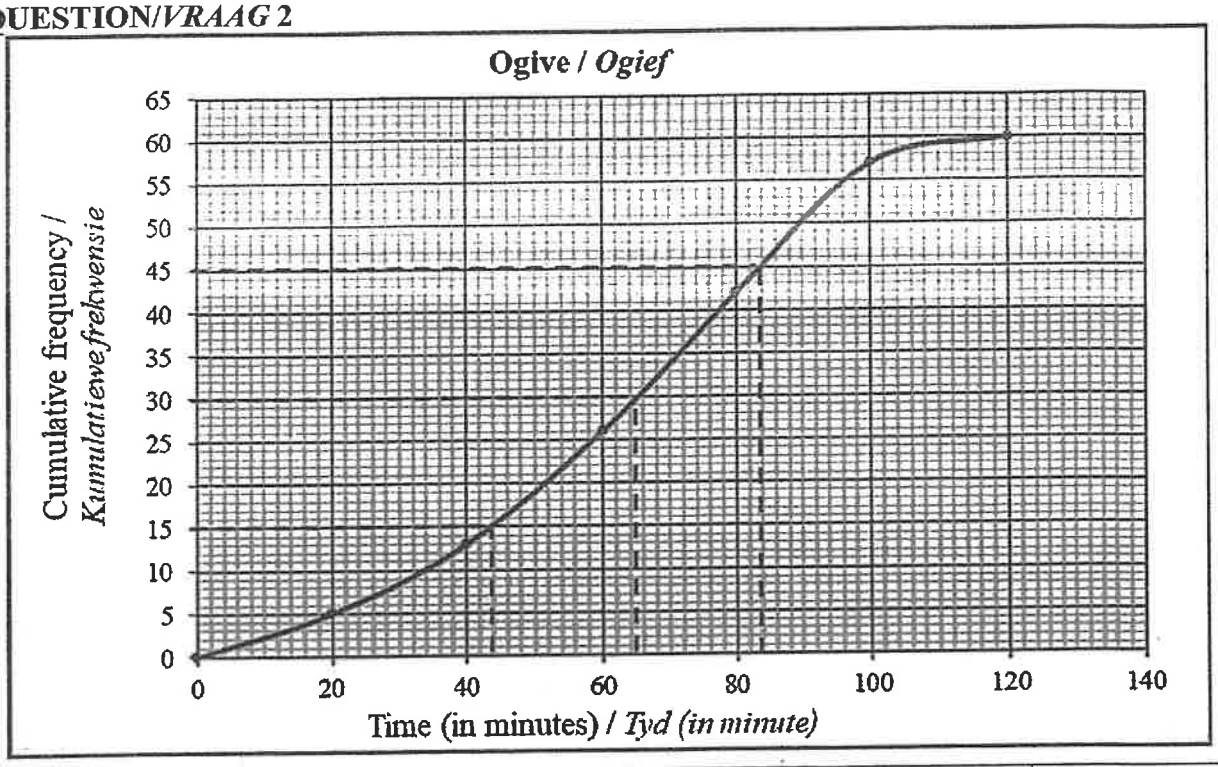
QUESTION/*VRAAG* 1

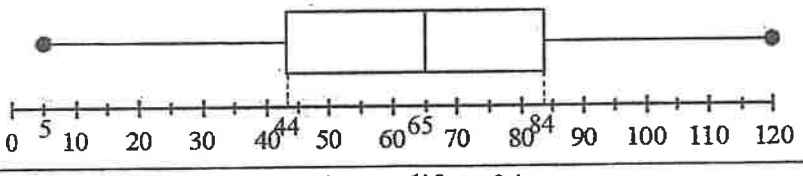
Weight (in kg) (x)	34	32	40	27	33	28	27	55	39	44	30	57	28	32	31
Number of push-ups per minute (y)	26	21	6	20	16	26	23	7	18	14	17	8	28	25	20



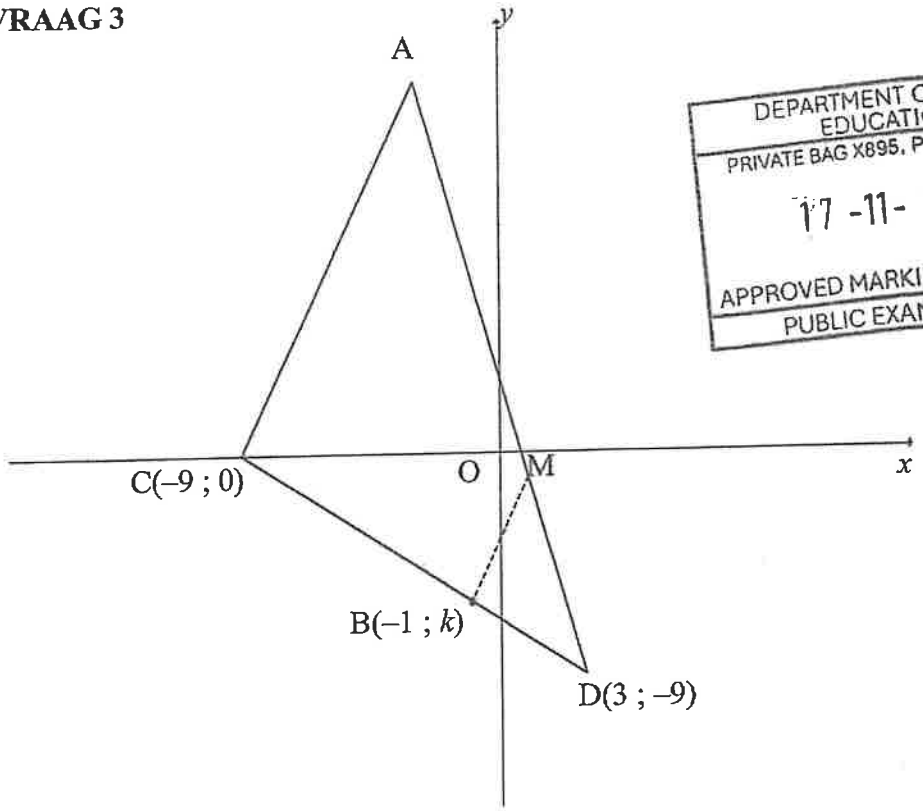
1.1	$a = 39{,}456001\ldots$ $b = -0{,}590018\ldots$ $\hat{y} = 39{,}46 - 0{,}59x$ CORRECT ANSWER ONLY: FULL MARKS	✓ $a = 39{,}46$ ✓ $b = -0{,}59$ ✓ equation (3)
1.2	$r = -0{,}8$	✓(A) $-0{,}8$ (1)
1.3	$y = 39{,}46 - 0{,}59(29)$ $y = 22{,}35$ **OR/*OF*** $y = 22{,}35$ (calculator)	✓ substitution ✓ answer (2) ✓✓ answer (2)
1.4	$\overline{y} = 18{,}33$	✓(A) 18,33 (1)
1.5	The increase in the number of push-ups will have **no influence**. The standard deviation **stays the same**.	✓ no influence **OR** standard deviation remains the same *geen verandering / bly dieselfde* (1)
1.6	6 is furthest y-value below the least squares regression line. An increase of 10 push-ups will get the team member to (40 ; 16), the minimum number of push-ups for a player weighing 40kg.	✓ 6 ✓ difference is 10 (2)
		[10]

QUESTION/*VRAAG* 2



2.1	Median = 65	✓ 65 (1)
2.2	$Q_1 = 44$	✓ 44 (1)
2.3	IQR = 84 – 44 = 40	✓ 84 ✓ IQR (2)
2.4		✓ box ✓(A) whiskers ending at 5 & 120 (2)
2.5	Number of employees who qualify = 34 % of employees who qualify $= \frac{34}{60} \times 100$ = 56,67% of the employees **OR/*OF*** Number of employees who qualify = 35 % of employees who qualify $= \frac{35}{60} \times 100$ = 58,33% of the employees	✓ 34 ✓ answer (2) ✓ 35 ✓ answer (2)
2.6	Number of intervals = 3 Time allowed to work from home = 3(30 minutes) = 90 minutes **OR/*OF*** 1,5 hours	✓ 3 ✓ answer (2)
		[10]

QUESTION / VRAAG 3

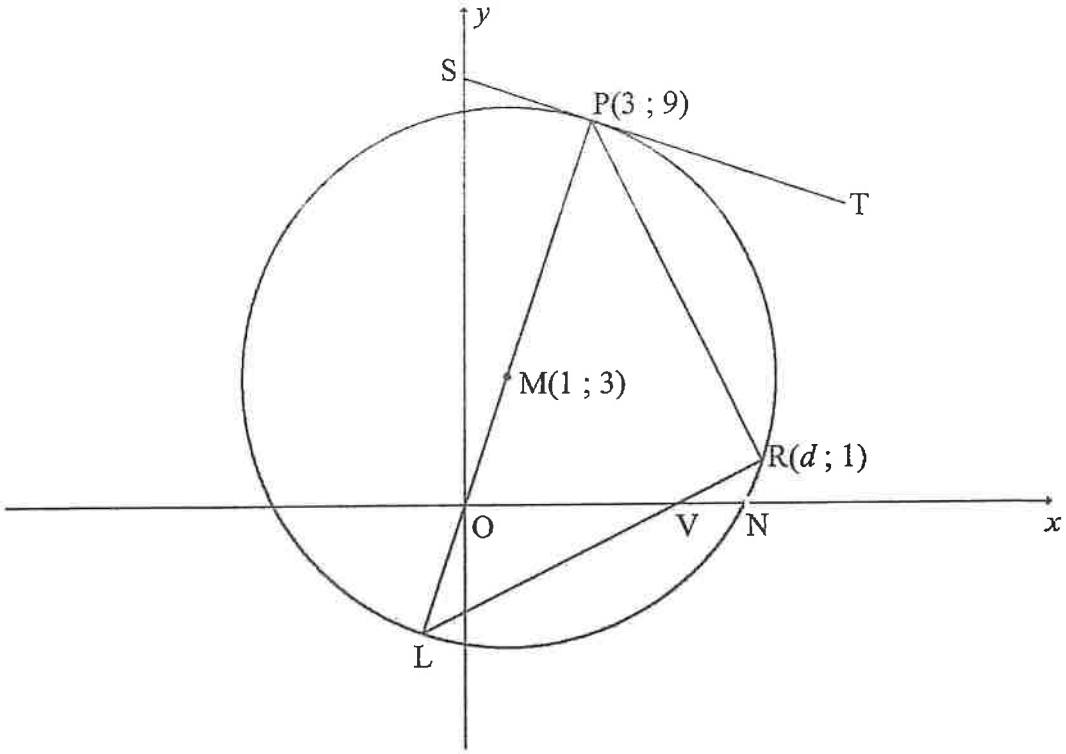


3.1	$m_{DC}=\frac{-9-0}{3-(-9)}$ **OR/*OF*** $m_{DC}=\frac{0-(-9)}{-9-3}$ $m_{DC}=-\frac{3}{4}$ $m_{DC}=-\frac{3}{4}$	✓ correct substitution of D(3;–9) & C(–9;0) into gradient formula ✓ answer (2)
3.2	Equation of DC: $0=-\frac{3}{4}(-9)+c$ **OR/*OF*** $y-0=-\frac{3}{4}(x-(-9))$ $c=\frac{-27}{4}$ or $-6\frac{3}{4}$ $y=-\frac{3}{4}(x+9)$ $y=-\frac{3}{4}x-\frac{27}{4}$ $y=-\frac{3}{4}x-\frac{27}{4}$	✓ correct substitution of C(–9;0) or D(3;–9) into equation of line ✓ answer (2)
3.3	$k=-\frac{3}{4}(-1)-\frac{27}{4}$ **OR/*OF*** $\frac{k-(-9)}{-1-3}=\frac{-3}{4}$ **OR/*OF*** $\frac{k-0}{-1-(-9)}=\frac{-3}{4}$ $k=\frac{3}{4}-\frac{27}{4}$ **OR/*OF*** $k+9=3$ **OR/*OF*** $k=-\frac{3}{4}(8)$ $k=-6$ $k=-6$ $k=-6$	✓ substitution of B(–1; *k*) (1)
3.4	$DC=\sqrt{(3+9)^2+(-9-0)^2}$ DC = 15 units	✓ correct substitution of D(3;–9) & C(–9;0) into distance formula ✓ answer (2)

3.5	$DB=\sqrt{\left(3-(-1)\right)^2+\left(-9-(-6)\right)^2}$ $DB = 5$ $\therefore \frac{DB}{DC}=\frac{5}{15}=\frac{1}{3}$	✓ DB = 5 ✓ answer (2)
3.6	$\frac{DM}{DA}=\frac{DB}{DC}=\frac{1}{3}$ $\frac{\text{Area } \Delta MBD}{\text{Area } \Delta ACD}=\frac{\frac{1}{2}(DM)(DB)\left(\sin \hat{D}\right)}{\frac{1}{2}(DA)(DC)\left(\sin \hat{D}\right)}$ $=\frac{1}{3}\times\frac{1}{3}$ $=\frac{1}{9}$	✓ $\frac{DM}{DA}=\frac{DB}{DC}$ ✓ correct use of area rule ✓ subst. for $\frac{BD}{DC}$ and $\frac{DM}{DA}$ into correct formula ✓ answer (4)
3.7	$y=-4x+c$ $m_{AD}=-4$ $-9=-4(3)+c$ $c=3$ $y=-4x+3$ $(x-3)^2+(y+9)^2=612$ $(x-3)^2+(-4x+3+9)^2=\left(\sqrt{612}\right)^2$ $(x-3)^2+(-4x+12)^2=612$ $x^2-6x+9+16x^2-96x+144=612$ $17x^2-102x-459=0$ $x^2-6x-27=0$ $(x-9)(x+3)=0$ $x=9$ or $x=-3$ N/A $y=-4(-3)+3$ $y=15$ A(–3 ; 15) **OR/*OF*** $\frac{y+9}{x-3}=-4$ $y+9=-4x+12$ $y=-4x+3$	✓ correct substitution of $m_{AD}=-4$ and D(3 ; –9) ✓ $(x-3)^2+(y+9)^2=612$ ✓ substitution of equation AD into distance formula ✓ standard form ✓ x values with rejection ✓ y coordinate (6)

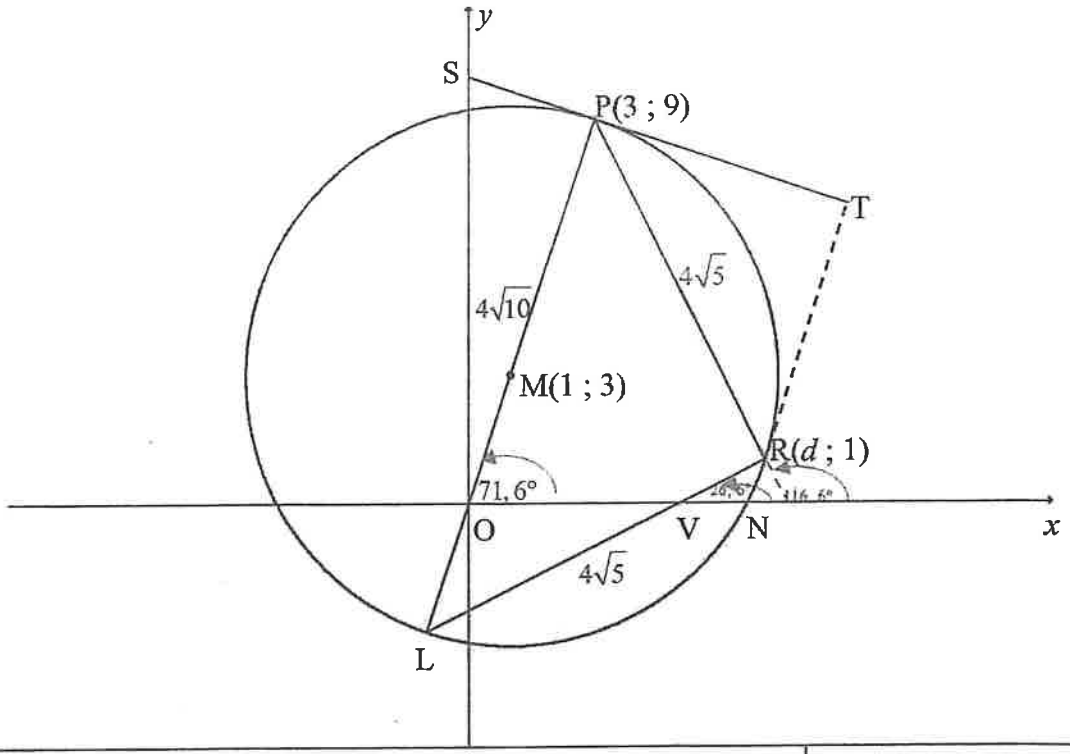
	OR/*OF*	**OR/*OF***
	$-9=-4(3)+c$	✓ correct substitution of $m_{AD}=-4$ and D(3 ; –9)
	$c=3$	
	$y=-4x+3$	
	N(0 ; 3)	✓ N(0 ; 3)
	$ND=\sqrt{(3-0)^2+(-9-3)^2}$	✓ substitution into distance formula to calculate ND
	$=3\sqrt{17}$	
	$AD=6\sqrt{17}$	
	$ND=\frac{1}{2}AD$	✓ $ND=\frac{1}{2}AD$
	N is the midpoint of AD	
	A(–3 ; 15)	✓ x – value ✓ y – value (6)
		[19]

QUESTION/*VRAAG* 4



4.1	L(–1 ; –3)	✓ $x=-1$ ✓ $y=-3$ (2)
4.2	$m_{MP}=\frac{9-3}{3-1}$ $m_{MP}=3$ $m_{ST}=-\frac{1}{3}$ $9=-\frac{1}{3}(3)+c$ $\quad$ $y-9=-\frac{1}{3}(x-3)$ $c=10$ **OR/*OF*** $y-9=-\frac{1}{3}x+1$ $y=-\frac{1}{3}x+10$ $\quad$ $y=-\frac{1}{3}x+10$	✓ $m_{MP}=3$ ✓ $m_{ST}=-\frac{1}{m_{MP}}$ ✓ substitution of m_{ST} & P(3; 9) into equation of a line ✓ equation of tangent ST (4)
4.3	$(x-1)^2+(y-3)^2=r^2$ $(3-1)^2+(9-3)^2=r^2$ $r^2=40$ $(x-1)^2+(y-3)^2=40$ $x^2-2x+1+y^2-6y+9=40$ $x^2+y^2-2x-6y-30=0$	✓ $(3-1)^2+(9-3)^2=r^2$ ✓ value of r^2 ✓ LHS of equation of circle ✓ expanding LHS (4)

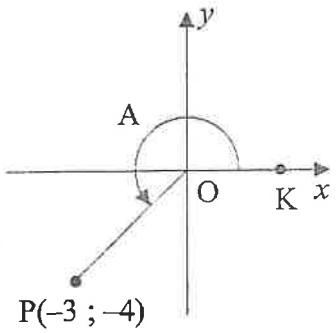
4.4	$d^2+(1)^2-2d-6(1)-30=0$ $d^2-2d-35=0$ $(d-7)(d+5)=0$ $d=7$ or $d=-5$ $\therefore d=7$ **OR/*OF*** $(x-1)^2+(y-3)^2=40$ $(d-1)^2+(1-3)^2=40$ $(d-1)^2=36$ $d-1=6$ or $d-1=-6$ $d=7$ or $d=-5$ $\therefore d=7$ **OR/*OF*** $P\hat{R}L=90°$ ($\angle$ in semi-circle) $\frac{9-1}{3-d}\times\frac{1-(-3)}{d-(-1)}=-1$ $d^2-2d-35=0$ $(d-7)(d+5)=0$ $d=7$ or $d=-5$ $\therefore d=7$	✓ $d^2+(1)^2-2d-6(1)-30=0$ ✓ standard form (2) **OR/*OF*** ✓ $(d-1)^2+(1-3)^2=40$ ✓ standard form (2) **OR/*OF*** ✓ $m_{PR}\times m_{RL}=-1$ ✓ standard form (2)

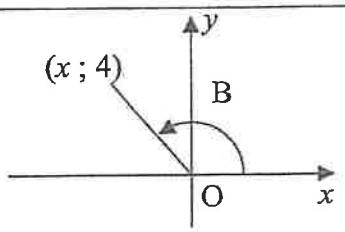


4.5	$m_{PO} = 3$ $\therefore \tan P\hat{O}V = 3$ $P\hat{O}V = 71{,}565...°$ $m_{RL} = \frac{1-(-3)}{7-(-1)}$ $= \frac{1}{2}$ $\therefore \tan R\hat{V}N = \frac{1}{2}$ $R\hat{V}N = 26{,}565...°$ $\hat{L} = 71{,}565...° - 26.565...°$ [ext. ∠ of Δ / *buite ∠ van* Δ] $\hat{L} = 45°$ **OR/*OF*** $\hat{R} = 90°$ [∠ in semi-circle /∠ *in 'n halwe sirkel*] $PR^2 = (3-7)^2 + (9-1)^2$ $PR = \sqrt{80} = 4\sqrt{5}$ units $PL^2 = (3-(-1))^2 + (9-(-3))^2$ **OR** $RL^2 = (7+1)^2 + (1+3)^2$ $PL = \sqrt{160} = 4\sqrt{10}$ $RL = \sqrt{80} = 4\sqrt{5}$ $\sin \hat{L} = \frac{4\sqrt{5}}{4\sqrt{10}}$ **OR** $\cos \hat{L} = \frac{4\sqrt{5}}{4\sqrt{10}}$ **OR** $\tan \hat{L} = \frac{4\sqrt{5}}{4\sqrt{5}}$ $\hat{L} = 45°$	✓ $\tan P\hat{O}V = m_{PO}$ ✓ $P\hat{O}V$ ✓ m_{RL} using R(7 ; 1) & L ✓ $R\hat{V}N$ ✓ answer (5) **OR/*OF*** ✓ $\hat{R} = 90°$ ✓ $PR = \sqrt{80} = 4\sqrt{5}$ ✓ length of PL **OR** RL ✓ trig ratio of $\hat{L}$ ✓ answer (5)

	OR/*OF*	**OR/*OF***
	$PL=\sqrt{(3+1)^2+(9+3)^2}=\sqrt{160}=4\sqrt{10}$	✓ length of PL
	$PR=\sqrt{(7-3)^2+(1-9)^2}=\sqrt{80}=4\sqrt{5}$	✓ $PR=\sqrt{80}=4\sqrt{5}$
	$LR=\sqrt{(7+1)^2+(1+3)^2}=\sqrt{80}=4\sqrt{5}$	✓ length of LR
	$\cos L=\frac{80+160-80}{2\sqrt{80}\times\sqrt{160}}$	✓ substitution into the cos rule
	$\cos L=\frac{\sqrt{2}}{2}$	
	$\hat{L}=45°$	✓ answer (5)
4.6	$m_{RM}=\frac{1-3}{7-1}$	
	$=-\frac{1}{3}$	✓ m_{RM}
	$m_{RT}=3$ (tan ⊥ rad)	✓ m_{RT}
	$m_{PT}=-\frac{1}{3}$	
	$m_{RT}\times m_{PT}=-1$	✓ $m_{RT}\times m_{PT}=-1$
	PT ⊥ RT	(3)
	OR/*OF*	**OR/*OF***
	$m_{MR}=\frac{3-1}{1-7}$	
	$=-\frac{1}{3}$	
	$m_{PT}=-\frac{1}{3}$ [proved in Q4.2]	
	$m_{PT}=m_{MR}$	
	∴PT ‖ MR	✓ PT ‖ MR
	$M\hat{R}T=90°$ [radius ⊥ tangent / *raaklyn ⊥ radius*]	✓ $M\hat{R}T=90°$
	$P\hat{T}R=90°$ [co-int ∠s; PT ‖ MR/*ooreenkomst. ∠e*; PT ‖ MR]	✓ $P\hat{T}R=90°$
	PT ⊥ RT	(3)
	OR/*OF*	**OR/*OF***
	$T\hat{P}R=\hat{L}=45°$ [tan-chord theorem/ *∠ tussen raaklyn en koord*]	✓ $T\hat{P}R=\hat{L}$
	TP = TR [tans from common pt]	
	∴ $T\hat{P}R=T\hat{R}P=45°$ [∠s opp equal sides/ *∠e teenoor gelyke sye*]	✓ $T\hat{P}R=T\hat{R}P$
	∴$P\hat{T}R=90°$ [sum of ∠s in Δ / *binne ∠e van Δ*]	✓ $P\hat{T}R=90°$
	PT ⊥ RT	(3)
		[20]

QUESTION/*VRAAG* 5



5.1.1	$r = 5$ $\cos A = -\frac{3}{5}$	✓ $r = 5$ ✓ answer (2)
5.1.2	$\cos 2A = 2\cos^2 A - 1$ $= 2\left(-\frac{3}{5}\right)^2 - 1$ $= -\frac{7}{25}$ **OR/*OF*** $\cos 2A = \cos^2 A - \sin^2 A$ $= \left(-\frac{3}{5}\right)^2 - \left(-\frac{4}{5}\right)^2$ $= -\frac{7}{25}$ **OR/*OF*** $\cos 2A = 1 - 2\sin^2 A$ $= 1 - 2\left(-\frac{4}{5}\right)^2$ $= -\frac{7}{25}$	✓ substitution of cos A into double angle formula ✓ answer (2) ✓ substitution of cos A & sin A into double angle formula ✓ answer (2) ✓ substitution of sin A into double angle formula ✓ answer (2)
5.1.3	 $x = -3$ $\sin(A-B) = \sin A\cos B - \cos A\sin B$ $= \left(-\frac{4}{5}\right)\left(-\frac{3}{5}\right) - \left(-\frac{3}{5}\right)\left(\frac{4}{5}\right)$ $= \frac{12}{25} + \frac{12}{25}$ $= \frac{24}{25}$	✓ $x = -3$ ✓✓ substitution into the compound angle formula ✓ answer (4)

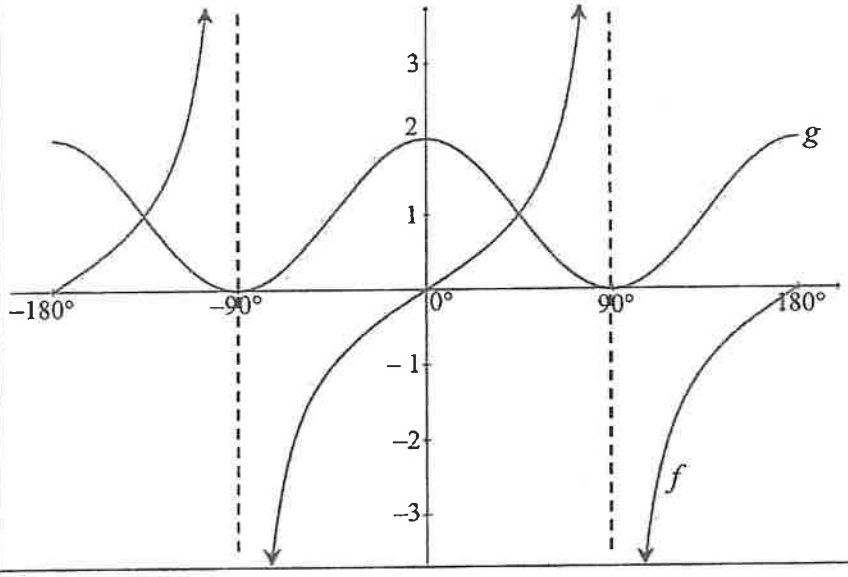
5.2	$\dfrac{\cos\left(\frac{\alpha}{2}-45°\right)\sin\left(\frac{\alpha}{2}-45°\right)}{2}$	
	$=\dfrac{2\cos\left(\frac{\alpha}{2}-45°\right)\sin\left(\frac{\alpha}{2}-45°\right)}{2.2}$	✓ multiply by $\frac{2}{2}$
	$=\dfrac{\sin(\alpha-90°)}{4}$	✓ double angle
	$=\dfrac{-\cos\alpha}{4}$	✓ co function
	$=\dfrac{-p}{4}$ **OR/*OF*** $=-\dfrac{1}{4}p$	✓ answer (4)
	OR/*OF*	**OR/*OF***
	$\dfrac{\cos\left(\frac{\alpha}{2}-45°\right)\sin\left(\frac{\alpha}{2}-45°\right)}{2}$	
	$=\dfrac{\left[\cos\frac{\alpha}{2}\cos45°+\sin\frac{\alpha}{2}\sin45°\right]\left[\sin\frac{\alpha}{2}\cos45°-\cos\frac{\alpha}{2}\sin45°\right]}{2}$	✓ expansion
	$=\dfrac{\left[\frac{\sqrt{2}}{2}\cos\frac{\alpha}{2}+\frac{\sqrt{2}}{2}\sin\frac{\alpha}{2}\right]\left[\frac{\sqrt{2}}{2}\sin\frac{\alpha}{2}-\frac{\sqrt{2}}{2}\cos\frac{\alpha}{2}\right]}{2}$	✓ special angles
	$=\dfrac{\frac{1}{2}\sin^2\frac{\alpha}{2}-\frac{1}{2}\cos^2\frac{\alpha}{2}}{2}$	
	$=\dfrac{-\frac{1}{2}\left(\cos^2\frac{\alpha}{2}-\sin^2\frac{\alpha}{2}\right)}{2}$	
	$=-\dfrac{\cos2\left(\frac{\alpha}{2}\right)}{4}$	✓ double angle
	$=-\dfrac{\cos\alpha}{4}$	
	$=-\dfrac{1}{4}p$	✓ answer (4)
		[12]

QUESTION/VRAAG 6

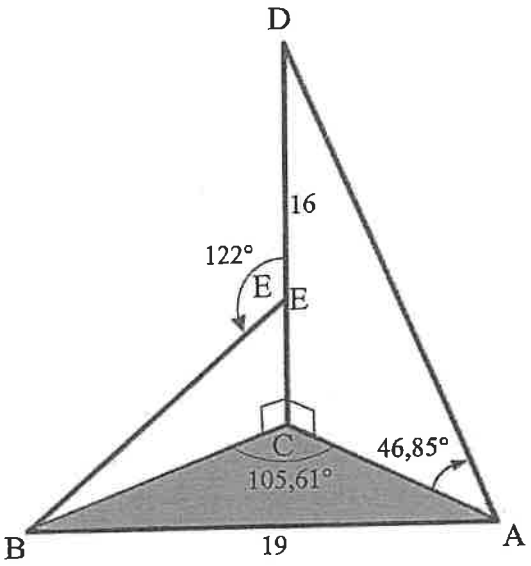
6.1.1	$\cos(x+y)=\cos(x-(-y))$ $=\cos x\cos(-y)+\sin x\sin(-y)$ $=\cos x\cos y-\sin x\sin y$	✓ $(x+y)=(x-(-y))$ ✓ correct expansion (2)
6.1.2	LHS $=\dfrac{\cos(90°-x)\cos y+\sin(-y)\cos(180°+x)}{\cos x\cos(360°+y)+\sin(360°-x)\sin y}$ $=\dfrac{(\sin x)\cos y+(-\sin y)(-\cos x)}{\cos x(\cos y)+(-\sin x)\sin y}$ $=\dfrac{\sin x\cos y+\cos x\sin y}{\cos x\cos y-\sin x\sin y}$ $=\dfrac{\sin(x+y)}{\cos(x+y)}$ $=\tan(x+y)$ = RHS	✓ $\cos(90°-x)=\sin x$ ✓ $\sin(-y)=-\sin y$ ✓ $\cos(180°+x)=-\cos x$ ✓ $\cos(360°+y)=\cos y$ ✓ $\sin(360°-x)=-\sin x$ ✓ compound angle formulae (6)
6.2	$\sqrt{6\sin^2 x-11\cos(90°+x)+7}=2$ $6\sin^2 x-11\cos(90°+x)+7=4$ $6\sin^2 x-11(-\sin x)+7=4$ $6\sin^2 x+11\sin x+3=0$ $(3\sin x+1)(2\sin x+3)=0$ $\sin x=-\dfrac{1}{3}$ **OR/*OF*** $\sin x=-\dfrac{3}{2}$ ref$\angle$ = 19,47° no solution $x=199{,}47°$ or $x=340{,}53°$	✓squaring both sides ✓ $\cos(90°+x)=-\sin x$ ✓ factors ✓ both equations ✓✓ answers (6)
6.3.1	$g(x)=\dfrac{4-8\sin^2 x}{3}$ $=\dfrac{4(1-2\sin^2 x)}{3}$ $=\dfrac{4\cos 2x}{3}$ Maximum value of cos 2x is 1 $\therefore$ maximum value of $g(x)=\dfrac{4}{3}$	✓ factors ✓ $\dfrac{4\cos 2x}{3}$ ✓ answer (3)

	OR/*OF*	**OR/*OF***
	$4-8\sin^2 x$ is a maximum when $\sin^2 x$ is a minimum	
	Minimum value of $\sin^2 x$ is 0	✓ min of $\sin^2 x = 0$
	$\therefore$ max. value of $g(x)=\frac{4-8(0)}{3}$	✓ $g(x)=\frac{4-8(0)}{3}$
	$g(x)=\frac{4}{3}$	✓ answer (3)
	OR/*OF*	**OR/*OF***
	$\sin x=\frac{-(0)}{2\left(-\frac{8}{3}\right)}$	✓ $\sin x=\frac{-(0)}{2\left(-\frac{8}{3}\right)}$
	$\sin x = 0$	✓ $\sin x = 0$
	$\therefore$ max. value of $g(x)=\frac{4-8(0)}{3}$	
	$g(x)=\frac{4}{3}$	✓ answer (3)
6.3.2	$x = 180°$	✓ 180° (1)
		[18]

QUESTION/*VRAAG* 7

7.1	$x = 90°$	✓ $x = 90°$ (1)
7.2	$x = -180°$ or $x \in (-90° ; 0°]$ **OR/*OF*** $x = -180°$ or $-90° < x \leq 0°$	✓✓ answer (2) ✓✓ answer (2)
7.3.1	$180°$	✓ answer (1)
7.3.2		✓ turning points on x-axis: $x = -90° ; 90°$ ✓ shape ✓ turning point on y-axis at $(0 ; 2)$ (3)
7.4	$2\cos^3 x - \sin x = 0$ $2\cos^3 x = \sin x$ $2\cos^2 x = \dfrac{\sin x}{\cos x}$ $2\cos^2 x = \tan x$ $2\cos^2 x - 1 = \tan x - 1$ $\cos 2x + 1 = \tan x$ $x = 45° + k.180°;\ k \in Z$ **OR/*OF*** $2\cos^3 x - \sin x = 0$ $\cos x\left(2\cos^2 x - \tan x\right) = 0$ $\cos x = 0$ or not valid or $2\cos^2 x = \tan x$ $2\cos^2 x - 1 + 1 = \tan x$ $\cos 2x + 1 = \tan x$ $x = 45° + k.180°;\ k \in Z$	✓ $2\cos^2 x = \tan x$ ✓ $2\cos^2 x - 1 = \tan x - 1$ ✓ $\cos 2x + 1 = \tan x$ ✓ answer (4) **OR/*OF*** ✓ $2\cos^2 x = \tan x$ ✓ $2\cos^2 x - 1 + 1 = \tan x$ ✓ $\cos 2x + 1 = \tan x$ ✓ answer (4)
		[11]

QUESTION/*VRAAG* 8



8.1	$\tan D\hat{A}C=\frac{DC}{AC}$ $AC=\frac{16}{\tan 46,85°}$ $AC=15\text{ m}$	✓ correct subs into trig ratio ✓ answer (2)
8.2	$(AB)^2=(BC)^2+(AC)^2-2(BC)(AC)\cos B\hat{C}A$ $(19)^2=x^2+(15)^2-2x(15)\cos 105,61°$ $x^2+8,07x-136=0$ $x=\frac{-8,07\pm\sqrt{(8,07)^2-4(1)(-136)}}{2(1)}$ $x=8,30\text{ m}$ or $x\neq -16,38\text{ m}$ $B\hat{E}C=58°$ **OR/*OF*** $E\hat{B}C=32°$ $\tan B\hat{E}C=\frac{BC}{EC}$ $\tan E\hat{B}C=\frac{EC}{BC}$ $EC=\frac{8,3}{\tan 58°}$ $EC=8,3\tan 32°$ $EC=5,19\text{ m}$ $EC=5,19\text{ m}$ $DE=10,81\text{ m}$ $DE=10,81\text{ m}$	✓ correct subst. into cosine rule ✓ quadratic equation in std form ✓ correct subst. into quadratic formula ✓ length of BC ✓ size of $B\hat{E}C$ **OR/*OF*** $E\hat{B}C$ ✓ length of EC ✓ answer (7)

OR/*OF*

$$\frac{\sin 105{,}61°}{19} = \frac{\sin C\hat{B}A}{15}$$

$C\hat{B}A = 49{,}5°$

$B\hat{A}C = 24{,}89°$

$$\frac{BC}{\sin 24{,}89°} = \frac{19}{\sin 105{,}61°}$$

$BC = 8{,}3$ m

✓ correct subst. into sine rule

✓ $B\hat{A}C$

✓ correct subst. into sine formula

✓ length of BC

$B\hat{E}C = 58°$

$$\tan B\hat{E}C = \frac{BC}{EC}$$

$$EC = \frac{8{,}3}{\tan 58°}$$

$EC = 5{,}19$ m

$DE = 10{,}81$ m

OR/*OF*

$E\hat{B}C = 32°$

$$\tan E\hat{B}C = \frac{EC}{BC}$$

$EC = 8{,}3 \tan 32°$

$EC = 5{,}19$ m

$DE = 10{,}81$ m

✓ size of $B\hat{E}C$ **OR/*OF*** $E\hat{B}C$

✓ length of EC

✓ answer

(7)

[9]

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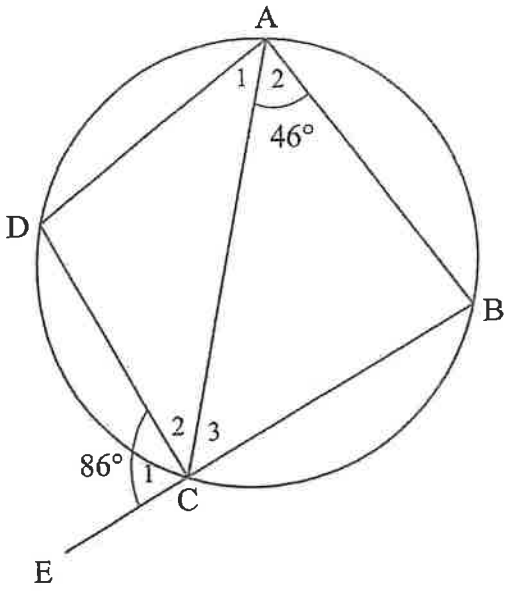
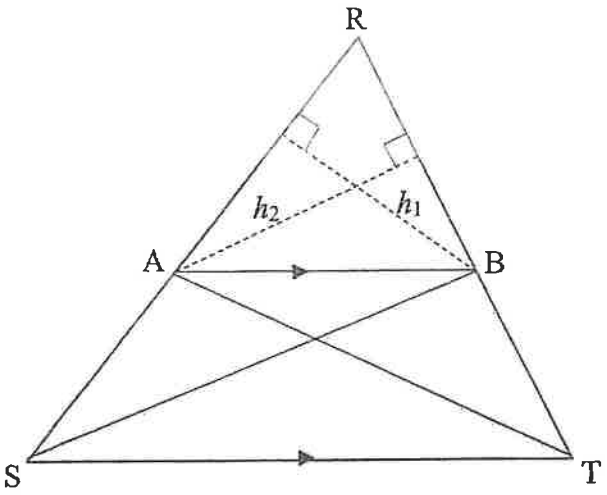
QUESTION/VRAAG 9



9.1	$\hat{A}_1 = 40°$ [ext. ∠ of a cyclic quad / *buite ∠ van kvh*]	✓S ✓R (2)
9.2	$\hat{B} = 80°$ $\left[\hat{A}_1 = \frac{1}{2}\hat{B}\right]$ $\hat{D} = 100°$ [opp ∠s of cyclic quad / *teenoorst. ∠e van kvh*] $\therefore \hat{C}_2 = 40°$ [sum of ∠s in Δ / *binne ∠e van Δ*] $\therefore \hat{C}_2 = \hat{A}_1 = 40°$ $\therefore AD = DC$ [sides opp = ∠s / *sye teenoor gelyke ∠*] **OR/*OF*** $\hat{B} = 80°$ $\left[\hat{A}_1 = \frac{1}{2}\hat{B}\right]$ $A\hat{C}E = \hat{A}_2 + \hat{B}$ [ext ∠ of Δ / *buite ∠ van Δ*] $\therefore \hat{C}_2 = 40°$ $\therefore \hat{C}_2 = \hat{A}_1 = 40°$ $\therefore AD = DC$ [sides opp = ∠s / *sye teenoor gelyke ∠*] **OR/*OF*** $\hat{B} = 80°$ $\left[\hat{A}_1 = \frac{1}{2}\hat{B}\right]$ $\therefore \hat{C}_3 = 180° - 46° - 80°$ [sum of ∠s in Δ / *binne ∠e van Δ*] $\therefore \hat{C}_3 = 54°$ $\therefore \hat{C}_2 = 180° - 86° - 54°$ [∠s on a str. line / *∠e op 'n reguitlyn*] $\therefore \hat{C}_2 = 40°$ $\therefore \hat{C}_2 = \hat{A}_1 = 40°$ $\therefore AD = DC$ [sides opp = ∠s / *sye teenoor gelyke ∠*]	✓S ✓S/R ✓S ✓R (4) ✓S ✓S/R ✓S ✓R (4) ✓S ✓S/R ✓S ✓R (4)
		[6]

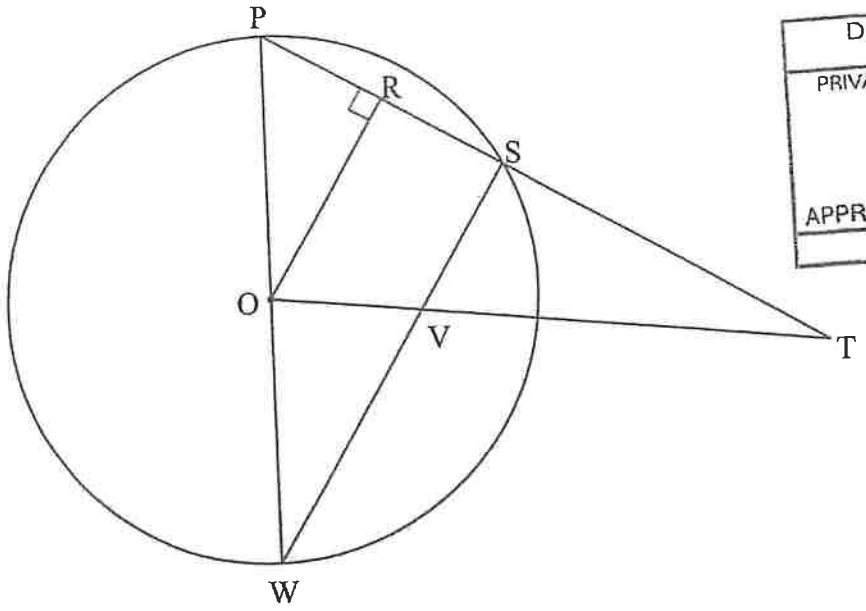
QUESTION/VRAAG 10

10.1



10.1	Construction: Join SB and TA and draw h_1 from B $\perp$ AR and h_2 from A $\perp$ RB *Konstruksie: Verbind SB en TA en trek h_1 vanaf B $\perp$ AR en h_2 vanaf A $\perp$ RB* Proof/*Bewys*: $\frac{\text{area } \Delta RAB}{\text{area } \Delta ASB} = \frac{\frac{1}{2}RA \times h_1}{\frac{1}{2}AS \times h_1} = \frac{RA}{AS}$ $\frac{\text{area } \Delta RAB}{\text{area } \Delta ABT} = \frac{\frac{1}{2}RB \times h_2}{\frac{1}{2}BT \times h_2} = \frac{RB}{BT}$ area ΔRAB = area ΔRAB [common/*gemeenskaplik*] But area ΔASB = area ΔABT [same base & height; AB || ST/ *dies. basis & hoogte; AB ||ST*] $\therefore \frac{\text{area } \Delta RAB}{\text{area } \Delta ASB} = \frac{\text{area } \Delta RAB}{\text{area } \Delta ABT}$ $\therefore \frac{RA}{AS} = \frac{RB}{BT}$	✓ construction ✓ $\frac{\text{area } \Delta RAB}{\text{area } \Delta ASB} = \frac{\frac{1}{2}RA \times h_1}{\frac{1}{2}AS \times h_1}$ ✓ $\frac{RA}{AS}$ ✓ $\frac{\text{area } \Delta RAB}{\text{area } \Delta ABT} = \frac{RB}{BT}$ ✓ S ✓ R (6)

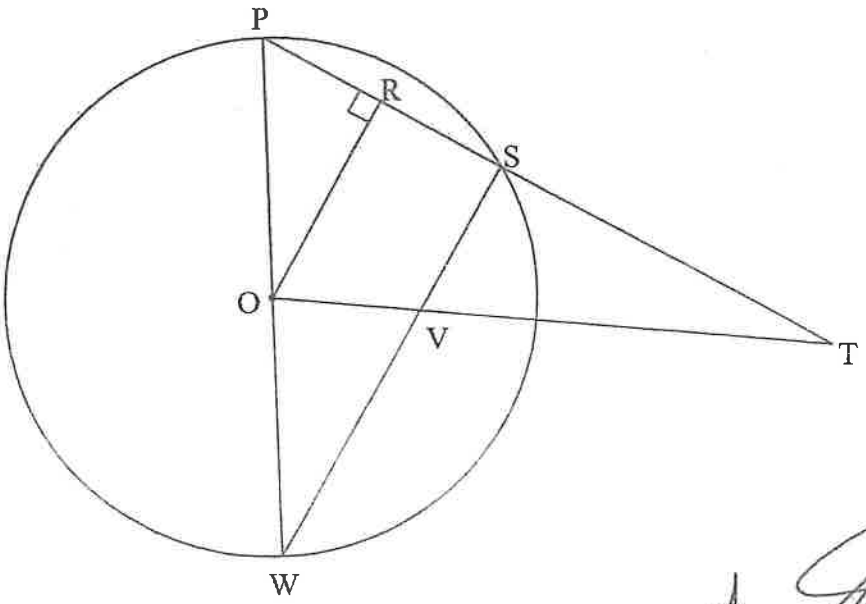
10.2



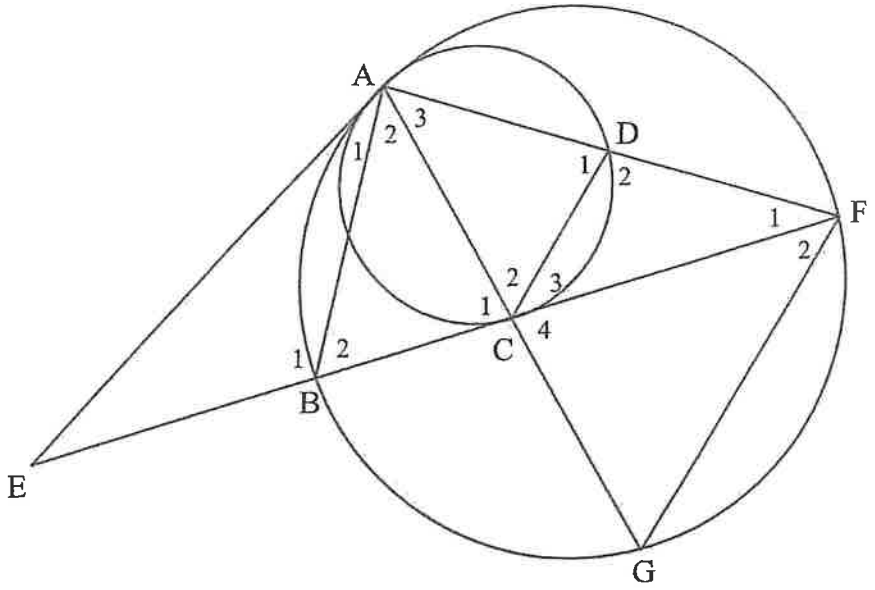
10.2.1	PR = RS	[line from centre ⊥ to chord/ *lyn vanuit midpt. sirkel ⊥ op koord*]	✓ S ✓ R
	PO = OW	[radii / *radiusse*]	✓ S
	$\therefore$ OR $= \frac{1}{2}$WS	[midpt theorem/*midpt. stelling*]	✓ S ✓ R
	$\therefore$ OR : WS = 1 : 2		(5)
	OR/*OF*		
	P$\hat{S}$W = 90°	[$\angle$ in semi circle/$\angle$ *in halwe sirkel*]	✓ S
	P$\hat{R}$O = 90°	[given]	
	$\therefore$ P$\hat{R}$O = P$\hat{S}$W		
	$\therefore$ RO || SW	[corresp $\angle$s = / *ooreenk.* $\angle e$ =]	✓ S
		OR/*OF*	
		[co-int. $\angle$s suppl / *ko-binne* $\angle e$ *suppl*]	
	$\frac{PO}{OW} = \frac{PR}{RS}$	[prop theorem; RO || SW/ *lyn* || *een sy van* Δ]	✓ S ✓ R
	PO = OW	[radii / *radiusse*]	
	$\therefore$ PR = RS		
	$\therefore$ OR : WS = 1 : 2	[midpt theorem/ *midpt. stelling*]	✓ R
			(5)

	OR/*OF*		
	ΔPRO and ΔPSW		
	$P\hat{S}W = 90°$	[$\angle$ in semi circle/$\angle$ *in halwe sirkel*]	
	$P\hat{R}O = 90°$	[given]	
	$\therefore P\hat{R}O = P\hat{S}W$		
	$\hat{P}$ is common		
	$P\hat{O}R = P\hat{W}S$	[sum of $\angle$s in Δ/ *som van* $\angle e$ *in* Δ]	
	$\therefore \Delta PRO \mid\mid\mid \Delta PSW$	[$\angle\angle\angle$]	✓ S ✓ R
	$\therefore \frac{PO}{PW} = \frac{RO}{SW}$	[$\mid\mid\mid$ Δs / $\mid\mid\mid$ Δe]	✓ S
	but $PW = 2\,PO$	[diameter = 2 radius/*middellyn = 2 radius*]	✓ S
	$\therefore \frac{RO}{SW} = \frac{PO}{2PO}$		✓ S
	$= \frac{1}{2}$		
	$\therefore$ OR : WS = 1 : 2		(5)
10.2.2	$\frac{OV}{VT} = \frac{RS}{ST} = \frac{1}{3}$	[prop theorem; RO $\|\|$ SW/ *lyn* $\|\|$ *een sy van* Δ]	✓ S /R
	$\frac{RS}{15} = \frac{1}{3}$		
	RS = 5 units		✓ S
	PR = RS = 5 units	[line from centre $\perp$ to chord / *lyn vanuit midpt. sirkel* $\perp$ *op koord*]	✓ S
	$\therefore$ PT = 25 units		✓ answer (4)
			[15]

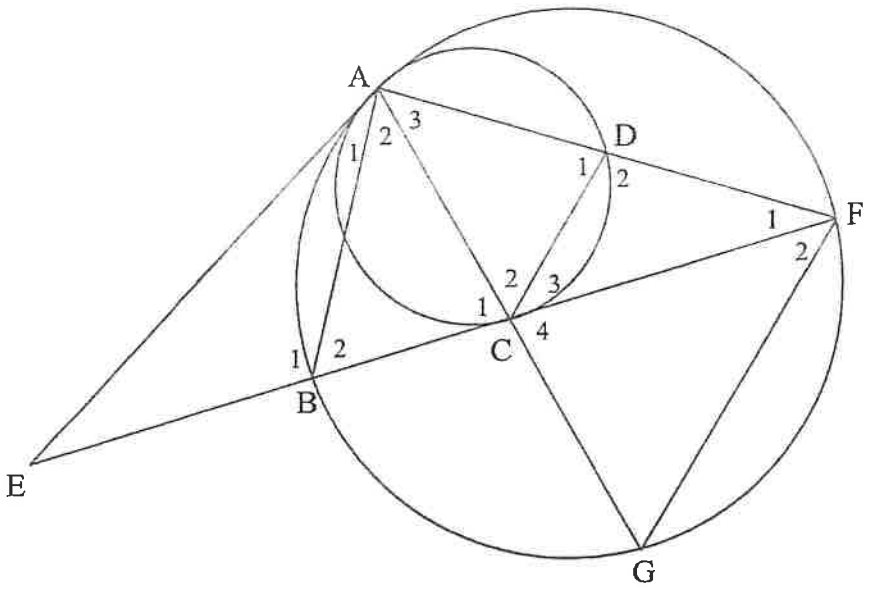
10.2



QUESTION/*VRAAG* 11



11.1	$\hat{D}_1 = E\hat{A}G = x$	[tan-chord theorem/ ∠ *tussen raaklyn en koord*]	✓ S ✓ R
	$\hat{C}_1 = \hat{D}_1 = x$	[tan-chord theorem/ ∠ *tussen raaklyn en koord*]	✓ S ✓ R
	$\hat{C}_4 = \hat{C}_1 = x$	[vert opp ∠s = / *regoorst. ∠e*]	✓ S/R
	$A\hat{F}G = E\hat{A}G = x$	[tan-chord theorem/ ∠ *tussen raaklyn en koord*]	✓ S (6)
	OR/*OF*		
	EA = EC	[tans from common pt/ *raaklyne vanuit dies. punt*]	✓ S/R
	$\hat{C}_1 = E\hat{A}G = x$	[∠s opp equal sides/ *∠e teenoor gelyke sye*]	✓ S
	$\hat{C}_4 = \hat{C}_1 = x$	[vert opp ∠s = / *regoorst. ∠e*]	✓ S/R
	$\hat{D}_1 = E\hat{A}G = x$	[tan-chord theorem/ ∠ *tussen raaklyn en koord*]	✓ S ✓ R
	$A\hat{F}G = E\hat{A}G = x$	[tan-chord theorem ∠ *tussen raaklyn en koord*]	✓ S (6)



11.2	$\hat{D}_1 = A\hat{F}G = x$		✓ S
	$\therefore$ DC ‖ FG	[corresp ∠s = / *ooreenk ∠e* =]	✓ S/R
	$\frac{AG}{AC} = \frac{AF}{AD}$	[prop theorem; DC ‖ FG / *lyn* ‖ *een sy van* Δ]	✓ S ✓ R
	$\therefore$ AG.AD = AC.AF		(4)
	OR/OF		
	In ΔACD and ΔAGF		
	$\hat{A}_3$ is common		✓ S
	$A\hat{F}G = \hat{D}_1 = x$	[proved in 11.1 / *reeds bewys*]	✓ S
	$\hat{C}_2 = A\hat{G}F = x$	[sum ∠ Δs/*binne ∠e Δ*]	
	ΔACD ||| ΔAGF	[∠∠∠]	✓ S/R
	$\frac{AC}{AG} = \frac{AD}{AF}$	[||| Δs $\therefore$ sides in proportion / ||| Δe $\therefore$ *sye in dieselfde verhouding*]	✓ S
	$\therefore$ AG.AD = AC.AF		(4)
11.3	In Δ AGF and ΔABC		
	$\hat{G} = \hat{B}_2$	[∠s in the same seg / *∠e in dies. segment*]	✓ S ✓ R
	$A\hat{F}G = \hat{C}_1 = x$	[proved in 11.1 / *reeds bewys*]	✓ S
	$\hat{A}_3 = \hat{A}_2$	[sum of ∠s in Δ/*binne ∠e van* Δ]	✓ S
	Δ AGF ||| ΔABC	[∠∠∠]	**OR/*OF*** R (4)

11.4	$\frac{GF}{BC}=\frac{AF}{AC}$ $[\Delta AGF \mid\mid\mid \Delta ABC]$	✓ S / R
	$\therefore GF=\frac{BC.AF}{AC}$	✓ S
	$\Delta ACD \mid\mid\mid \Delta FGC$ $[\angle\angle\angle]$	✓ S
	$\therefore \frac{AC}{GF}=\frac{AD}{FC}$	✓ S
	$\therefore AC=\frac{AD.FG}{FC}$	
	$\therefore GF=BC.AF\div\frac{AD.FG}{FC}$	✓ S
	$GF=BC.AF\times\frac{FC}{AD.FG}$	✓ S
	$\therefore GF^2=\frac{BC.FC.AF}{AD}$	(6)
	OR/*OF*	**OR/*OF***
	$\Delta AGF \mid\mid\mid \Delta ABC$ $[\angle\angle\angle]$	
	$\frac{GF}{BC}=\frac{AF}{AC}$	✓ S
	$GF=\frac{AF.BC}{AC}$	✓ S
	$\Delta ACD \mid\mid\mid \Delta AGF$ $[\angle\angle\angle]$	
	$\frac{AD}{AF}=\frac{CD}{GF}$	
	$GF=\frac{AF.CD}{AD}$	✓ S
	$GF\times GF=\frac{AF.BC}{AC}.\frac{AF.CD}{AD}$	✓ S
	$\Delta FCD \mid\mid\mid \Delta FAC$ $[\angle\angle\angle]$	✓ S
	$\frac{FC}{FA}=\frac{CD}{AC}$ from $\mid\mid\mid \Delta$`s	
	$FC=\frac{CD.AF}{AC}$	✓ S
	$GF^2=\frac{AF.FC.BC}{AD}$	(6)
		[20]

TOTAL/*TOTAAL*: 150

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DEPARTMENT OF BASIC EDUCATION
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17 -11- 2024
APPROVED MARKING GUIDELINE
PUBLIC EXAMINATION

TOLERANCE RANGE: 2024 OCTOBER/NOVEMBER EXAMINATION

SUBJECT	MATHEMATICS			PAPER	2								
QUESTION NUMBER	Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9	Q10	Q11		
MAX MARK	10	10	19	20	12	18	11	9	6	15	20		
TOLERANCE RANGE PER QUESTION *Indicate the item at which the Tolerance Range will apply*				4.5 (1)				8.2 (1)			11.2 (1)		
				4.6 (1)									
OVERALL TOLERANCE RANGE FOR QUESTION PAPER	4 marks (2,67%)							TOTAL MARKS			150		

APPROVED

DBE: Approved DBE IM.

DATE: 2024 – 11 – 14

UMALUSI: Approved Umalusi Moderator Mr. M. Govender 14/11/2024

Approved Mr. R. Govender 14/11/2024 Umalusi Moderator.